

Differential Raytracing for Exact Radiometric Calculations

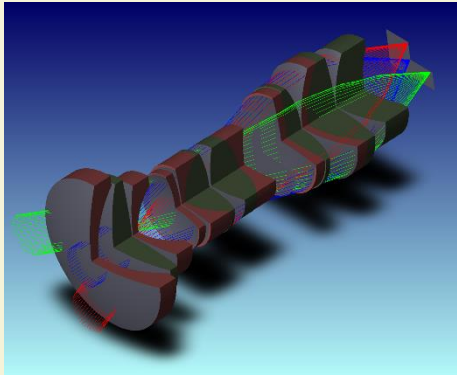
M. Jahny, B. Michel
Hembach Photonik GmbH

116. DGaO Annual Meeting, Brno, 27.05.2015

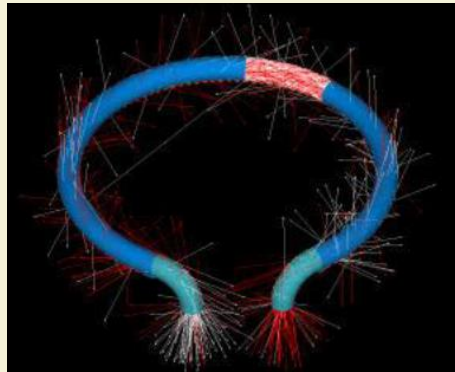
Hembach Photonik GmbH

Key Areas

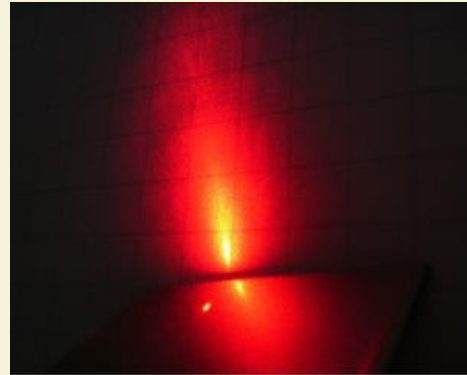
Imaging optics



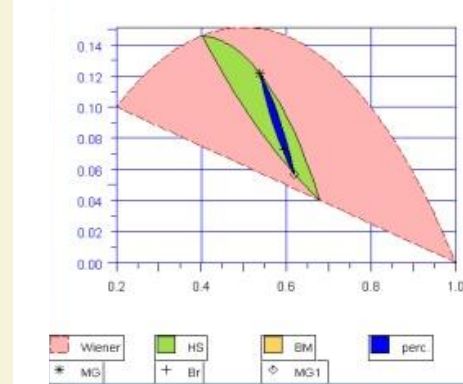
Illumination optics



Straylight analysis



Software development



Small innovative company in **Nürnberg Area**, Germany

Currently 8 employees: physicists, mathematicians and engineers

Optical design and analysis for customers

Hembach **Photonik**

Overview

- Idea of differential raytracing
- Advantages of differential raytracing
- Example: Point light source
- Example: Collimated light source
- Applications and limitations



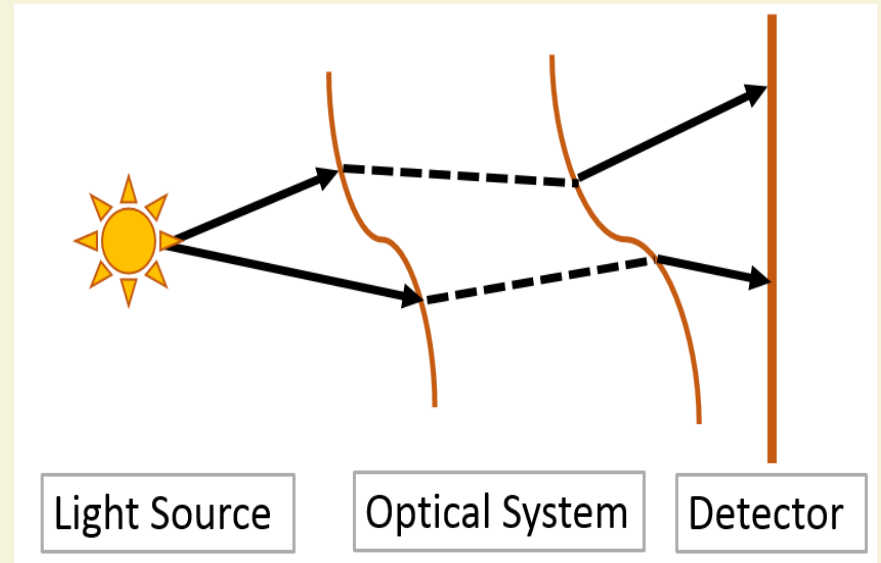
Motivation for Differential Raytracing

Non-Sequential Raytracing:

Compute radiometric quantities by tracing rays through optical systems

Conventional Raytracers

- Tracing of randomly generated rays (Monte-Carlo-method)
- Accuracy and computational time depend on number of rays

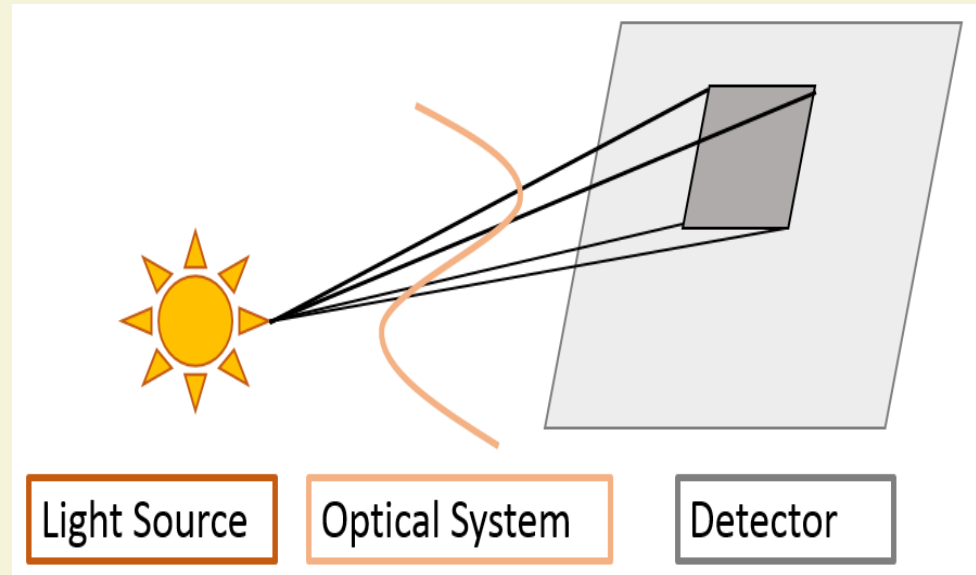


Idea of Differential Raytracing

- Trace ray bundles instead of single rays
- Ray bundles contain differential information

This enables us to:

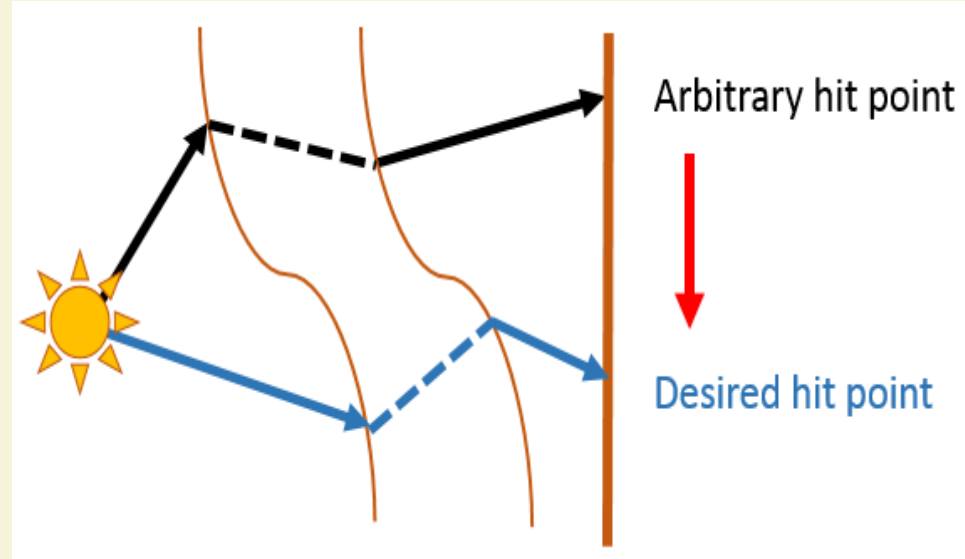
- Move rays on detector
- Obtain exact irradiance value



Reaching All Detector Points

Vary ray bundle to possible hit points while keeping the start point

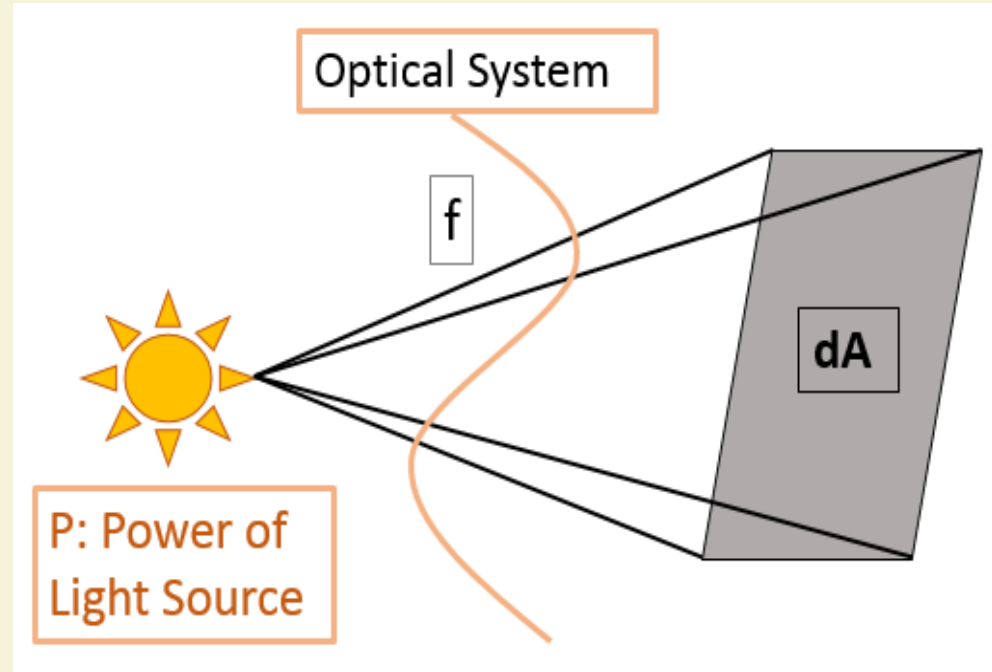
Consequence:
All possible detector points are reached



Getting Exact Irradiance Values

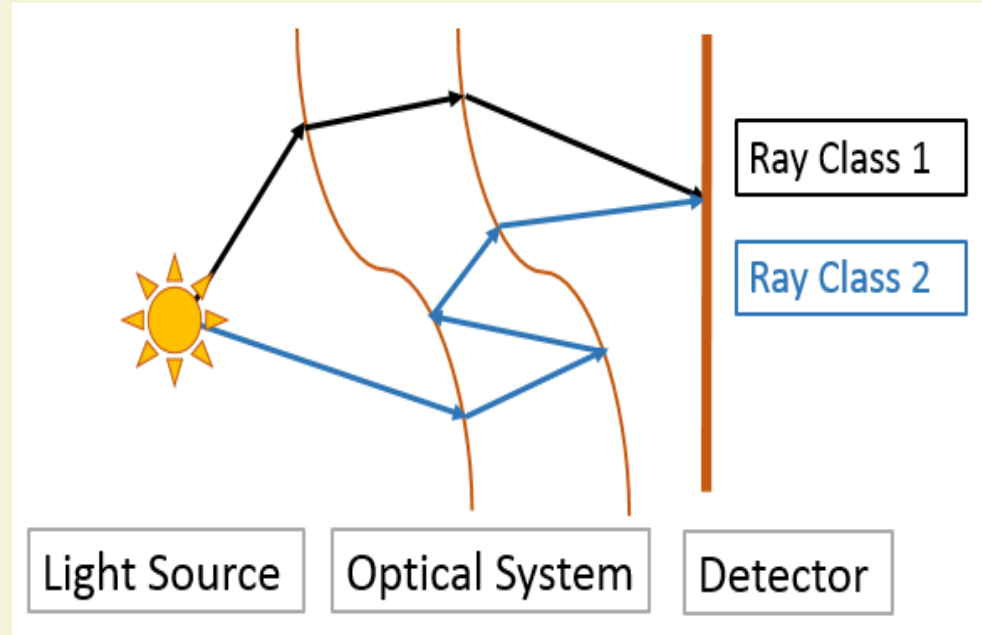
- **f**: Function describing optical system
- **Area dA**: Given by Jacobi-determinant of function f
- **Irradiance**: $E = \frac{dP}{dA}$

Consequence:
Information about derivatives of f leads to exact irradiance values



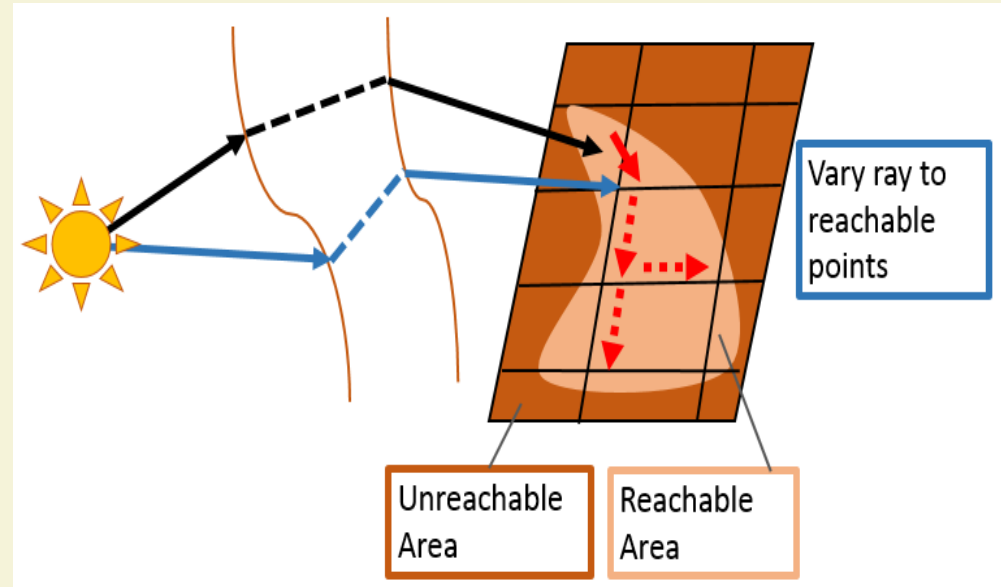
Equivalence Classes

- Specify equivalence classes for rays:
 - Number of hits
 - Hit objects
 - Start direction
 - Start point
 - ... and other criteria
- Only one ray per equivalence class gives irradiance on reachable detector points

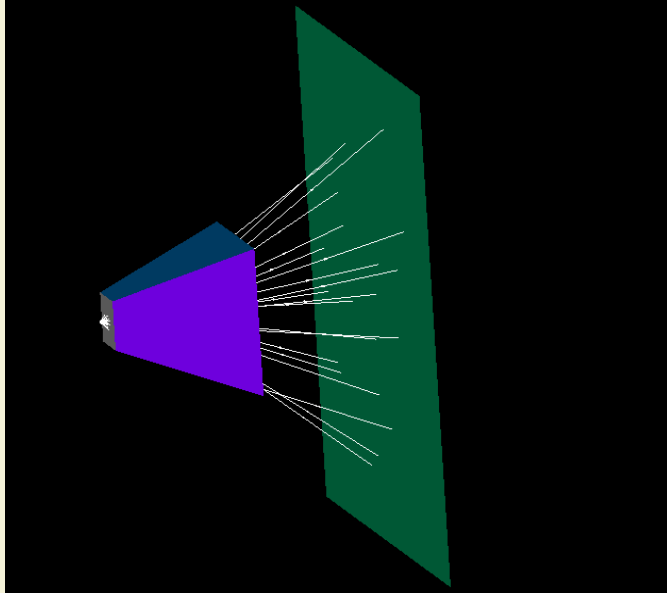


Advantages of Differential Raytracing

- Significant reduction of number of rays
- Consideration of all accessible detector points
- Exact irradiance value on all points

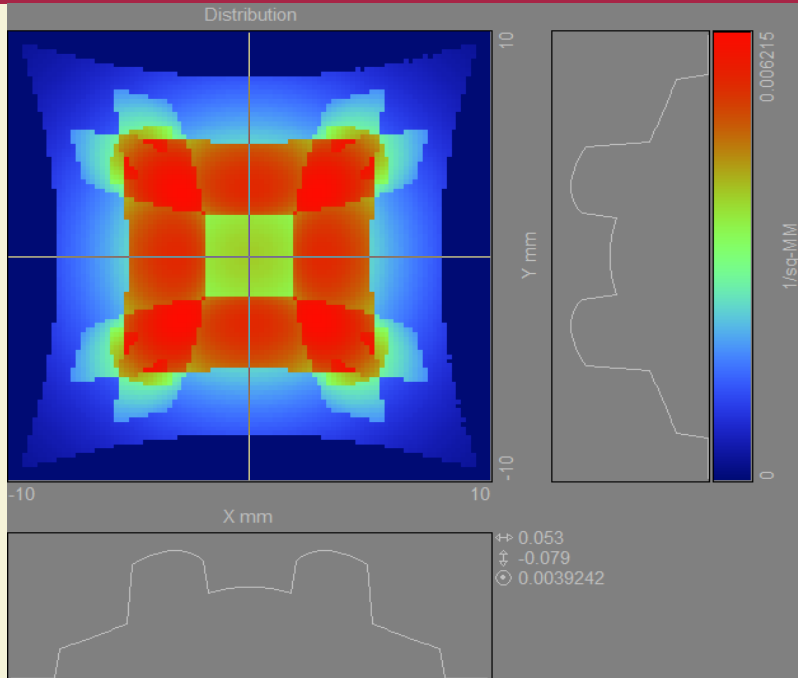


Example: Point Light Source

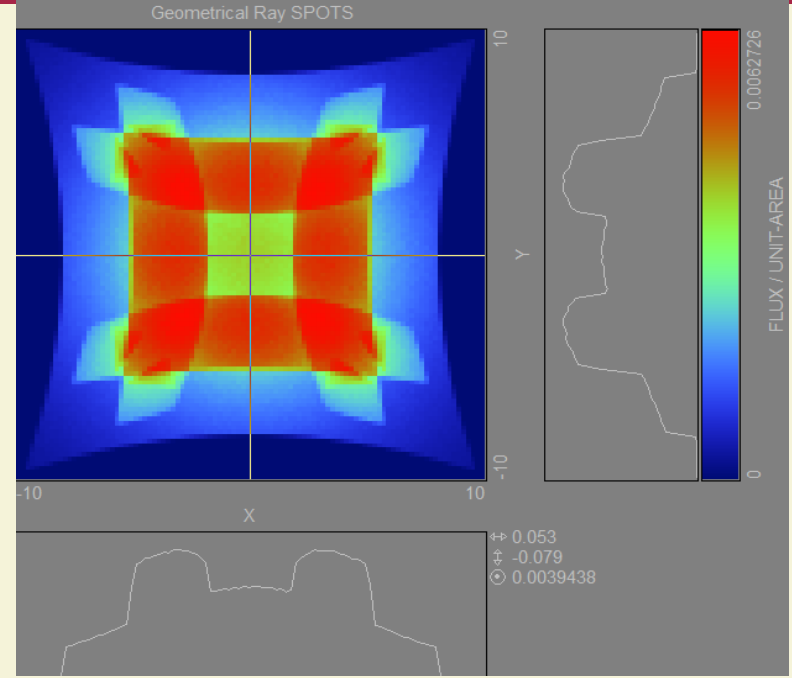


- Point light source
- Frustum (PMMA)
- Detector
- System with 9 relevant ray paths

Irradiance on Detector



Differential raytracing, 10^3 rays



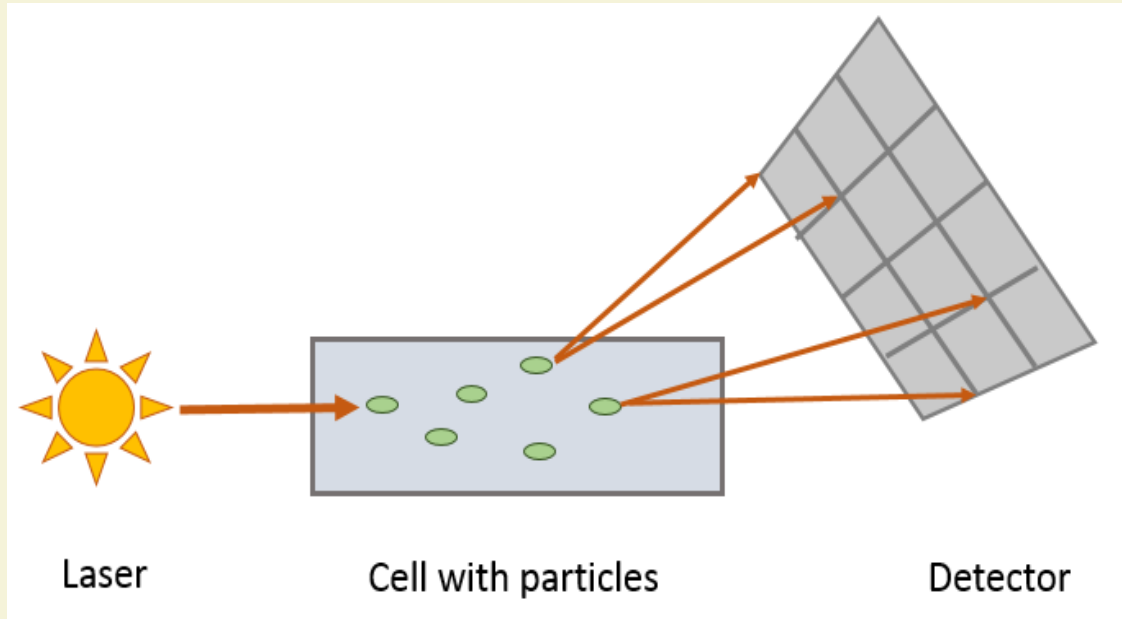
ASAP, 10^8 rays

Example: Extended Light Source

Laser sends ray on particles in a measuring cell

Particles send light to detector as one extended light source

Vary rays on detector to compute scattered power on detector

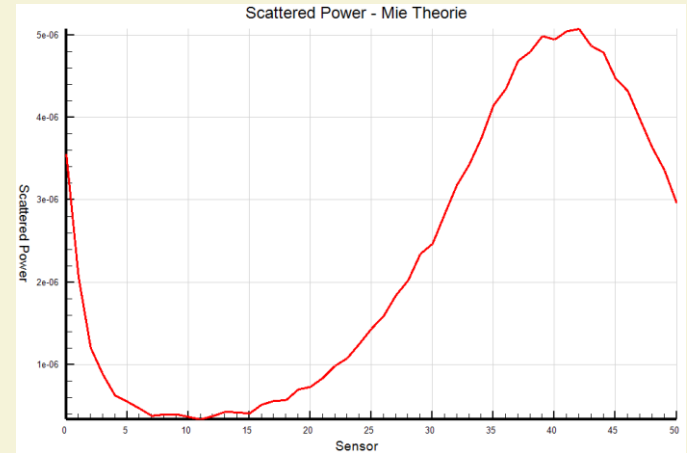


Scattered Power

- **Scattered Power P_{det}** : Function of Scattering function and detector area
- **Detector area** given by Jacobi-determinant **$J(r)$**
- **Scattering function $S(\Theta, \varphi)$**
from Mie- or Fraunhofer Theory
- **$T(\Theta, \varphi)$** : Losses from transmission

$$P_{det} = \int_{z,A} T(\theta, \varphi) S(\theta, \varphi) |J(r)|^{-1} d(z, A)$$

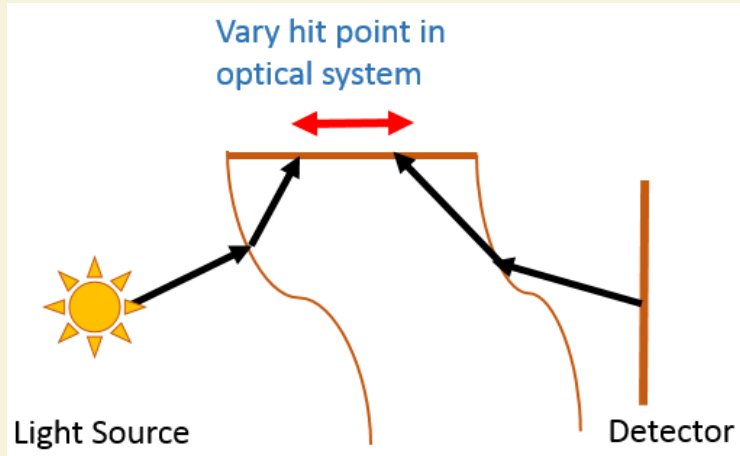
Scattering Power on 50 detectors with Mie-Theory



Applications and Limitations

Applications

- Stray light analysis



- ... and many more

Open tasks / Limitations

- Unique identification of ray classes
- Classification of singularities
- Useful if number of ray paths not too big
- Design tool rather than analysis tool

